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### PRACE INSTYTUTU MASZYN PRZEPŁYWOWYCH

poświęcone są publikacjom naukowym z zakresu teorii i badań doświadczalnych w dziedzinie mechaniki i termodynamiki przepływów, ze szczególnym uwzględnieniem problematyki maszyn przepływowych

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#### JOACHIM RAABE, JANUSZ STELLER

Institut für hydraulische Maschinen und Anlagen, Technische Universität München (Institute of Hydraulic Machinery and Equipment, Technical University of Munich)

Instytut Maszyn Przepływowych PAN, Gdańsk (Institute of Fluid-Flow Machinery, Polish Academy of Sciences, Gdansk)

### A Simplified Approach to Predict Some Cavitation Effects at the Axial Runner Vanes

single bubble model is used to predict cavitation erosion zones at an axial runner vane under and to derive a scaling law on cavitation erosion rate.

### **1. Introduction**

merous reports on model tests of hydraulic machinery [1,2,3] indicate at an dy cavitation cloud consisting of a multitude of small cavities as an especially non form of cavitation at the runner vanes. It is quite obvious that this form tation is responsible for most of blade erosion and contributes significantly thine vibration and some fatigue fractures of the vanes. Significant progress ten recently made in our understanding of the phenomenon. This is due both experimental research on cavitation cloud structure [4] and dynamics [5] and the theoretical efforts in this respect [6, 7, 8]. However, there is still lack of the method that would allow to predict various aspects of bubble cavitation draulic machine. A lot of cavitation prediction work as well as many research aiming to correlate selected cavitation aspects with operating conditions and cometry of a hydraulic machine (or a ship propeller) are still based on single evolution models [9, 10]. Despite of rather rough approximations, these often prove to be unexpectedly efficient.

decently, one of the authors developed a simplified model of single bubble evo-— originally proposed by A. D. Pernik [11] — in order to predict cavitation zones at the blade sections of hydraulic machines [12, 13]. Theoretical results satisfactory agreement with experiment and the results of an inspection under conditions. A single bubble model was also used later on to derive a scaling law meming cavitation erosion of Kaplan runner vanes [14]. A critical summarization bitherto obtained results is given in the present report.

### 2. Cavitation Extent Prediction by Means of a Simplified Model of Single Bubble Evolution

The model used in this paper has been already discussed in detail in Ref. [12] and [13]. The basic idea consists in dividing the bubble evolution process into threstages, that is the rise in the region of local pressure p, being lower than the saturated vapour pressure  $p_v$ , the rise in the region of local pressure being higher than the saturated vapour pressure and the collapse of the bubble. In each of the stages the realistic pressure distribution is replaced by its mean value (Fig. 1). The position  $s_0$  of the bubble at the end of the first stage is determined by the equality  $p = p_0$ . The positions  $s_2$  and  $s_3$ , at the end of the second and the third stage, respective can be found from the simplified solutions of the Rayleigh equation [11] and the assumption of no slip between the bubble and surrounding liquid [12, 13]. Both the bubble radii and respective bubble positions for a fixed flow pattern and a giver cavitation number appear to be proportional to the characteristic dimension the flow system (e.g. blade section chord or tip diameter of the runner).

The method has been applied successfully for cavitation prediction under laboratory conditions and at the guide vanes of a pump-turbine in Żydowo Pumped Storag Power Plant in Pomerania (Poland) [12, 13]. Recently, it was also used to predicavitation erosion zones at the runner vanes of a Kaplan turbine at the Berghein Power Plant, arranged in a cascade of four river power plants at the German Danuar (Fig. 2 [15]). The Bergheim Plant consists of three units of tip diameter D = 5.35 and rated capacity P = 8.25 MW, operating under rated head H = 5.97 m. Rate suction head — taken as the runner exit height above the tailwater level — amount  $H_s = 1.15$  m. Rotation speed, n = 76.9 rpm, is compatible with f = 16 2/3 Hz frequency of the West German railroad traction grid. The varying power deman of the traction grid requires sometimes an off-design point of operation with hearising up to 8.5 m and the tail water level falling even 1.5 m below its standard level.









Fig. 2. Cascade of four river plants at the German Danube (after [15])

During a period of 48 500 hours of operation the suction face of 4 runner vanes and a remarkable pitting area, especially at the cylindrical section of 95% of the tip diameter. This is attributed to 12 800 hours of swell operation, in particular H = 8.5 m head, Q = 106.2 m<sup>3</sup>/s flow rate and an angle of  $\varphi = 16^{\circ}$ , the chord D cylindrical blade section makes with the circumference. Velocity distrition round this blade section has been calculated by means of the Schlichting's calarity method [16] at the Technical University of Munich. Operation point and blade geometry data have been delivered by the power plant owner (Rhein-Maindenau AG) and the turbine producer (J. M. Voith GmbH), respectively.

Cavitation inception number,  $\sigma_i$ , has been calculated from the formula [17]

$$\sigma_i = \lambda_{\max} \frac{w_1^2}{2gH} + \eta_s \frac{c_m^2}{2gH} \tag{1}$$

w<sub>1</sub> and  $c_m$  are the relative and the absolute meridional velocity at the runner respectively, g is the acceleration of gravity and  $\eta_s$  — the draft tube efficiency. pressure coefficient,  $\lambda$ , can be found from the distribution of the relative velousing the formula

$$\lambda = (w/w_1)^2 - 1 - K_0$$
<sup>(2)</sup>

 $K_0$  denotes a coefficient accounting for the height of the actual point above maner outlet 1, and the respective runner losses [14]. Installation sigma,



Predicted and realistic erosion zone at the runner vane in Bergheim Power Plant photograph by Rhein-Main-Donau AG)

#### $\sigma = \text{NPSH}/H$

proved to be smaller than cavitation inception number  $\sigma_i$ , which indicated that cavitation should have been expected. In fact erosion zone calculation by means of the simplified model of single bubble evolution coincided well with the results of field inspection (Fig. 3).

### 3. Erosion Rate — a Scaling Law Following from the Analogy Between Cavitation and Liquid Impact Damage

We shall assume further on that cavitation damage is due to the collapse of individual bubbles travelling with the velocity of surrounding liquid and not interacting one with another. The number of cavities or cavitation nuclei in a unit mass of fluid will be considered constant. All the supercritical nuclei will be assumed equivalent, that is having equal gas content and following Rayleigh equation without viscosity, surface tension and gas diffusion terms. For simplicity, we shall assume the isothermal gas convertion inside a bubble with  $R_0$  being the bubble radius corresponding to the partial gas pressure  $\Delta p_0$  under steady-state conditions.

Under these assumptions, the Rayleigh model yields the following formula for the bubble collapse rate [18]

$$\dot{R}^2 = \frac{2\Delta p}{3\rho} \left[ \left( \frac{R_a}{R} \right)^3 - 1 \right] - \frac{2\Delta p_0}{\rho} \left( \frac{R_0}{R} \right)^3 \ln \frac{R_a}{R}$$
(4)

where  $\Delta p = p - p_v$  and the subscript *a* corresponds to the start of the collapse. The local pressure *p*, is assumed to be kept constant during the collapse. It followeasily from Eq. (4) that the maximum collapse rate, corresponding to the bubble radius

$$R_{i} = R_{0} \sqrt[3]{\Delta p_{0}/\Delta p} = R_{0} \sqrt[3]{(2\Delta p_{0}/\rho w_{1}^{2})/(K_{1}-\lambda)}$$
(5)

can be calculated from the formula

$$\dot{R}_{i}^{2} = \frac{2\Delta p}{3\rho} \left( \frac{\Delta p R_{a}^{3}}{\Delta p_{0} R_{0}^{3}} - 1 - \ln \frac{\Delta p R_{a}^{3}}{\Delta p_{0} R_{0}^{3}} \right)$$

where parameter  $K_1$  in Eq. (5) denotes cavitation index,

$$K_1 = (p_1 - p_v) / (0.5\rho w_1^2)$$

defined by pressure  $p_1$ , and relative velocity  $w_1$ , at the runner outlet. Disregarding the last two terms in the parantheses in Eq. (6) yields

$$\dot{R}_{i} = \Delta p \sqrt{\frac{2R_{a}^{3}}{3\rho \Delta p_{0}R_{0}^{3}}} = 0.5w_{1}^{2}(K_{1} - \lambda) \sqrt{\frac{2\rho R_{a}^{3}}{3\Delta p_{0}R_{0}^{3}}}.$$

The corresponding kinetic energy of the liquid around the collapsing bubble becomes, according to Rayleigh

$$E_{\rm kin.} = 2\pi\rho R_1^{3} \dot{R}_i^{2} = (2\pi/3)\rho w_1^{2} R_a^{3} (K_1 - \lambda_i).$$

(3)

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In fact, the Rayleigh model used above assumes spherical symmetry. On the ther hand side, cavitation pitting is generally acknowledged nowadays to be mainly to the cumulative jets forming during bubble collapses close to a solid wall. The energy delivered to the wall by a cavitation microjet is a fraction of the total metic energy of the liquid surrounding the collapsing bubble. No serious error to be done by assuming this energy to be proportional to the energy calculated the Eq. (9). In the same way we shall assume the average realistic "effective" microvelocity to be proportional to the maximum collapse rate as calculated from Eq. (8).

The energy needed for cavitation erosion of  $\Delta V$  volume of the wall material given by equation

$$\Delta E = \mathcal{R}_{cav} \Delta V \tag{10}$$

the  $\Re_{cav}$  denotes the so called cavitation resistance. In general,  $\Re_{cav}$  depends both the structure of cavitation pulses and on the physical and chemical features of interial which change significantly in course of cavitation attack [19]. It follows the considerations of F. G. Hammitt et al [20] that the initial value of caviresistance is usually close to the ultimate resilience

$$UR = 0.5\sigma_R^2 / \xi \tag{11}$$

 $\sigma_R$  denotes the tensile strength and  $\xi$  is the Young modulus of the material. The result coincides with the result of theoretical considerations presented in Ref. [14] and assumption of a rather special erosion mechanism.

The average volume loosened by a single collapse can be thus expressed as

$$V = \eta E_{\rm kin} / \mathscr{R}_{cav} \tag{12}$$

being the proportionality coefficient between energy delivered to the solid be energy following from Eq. (9). Under assumptions made before there are

$$\Delta N = \Delta b \,\Delta t \int_{0}^{\infty} \mathcal{N} w \,dn \tag{13}$$

collapses to be expected in a time interval  $\Delta t$  over a blade strip of  $\Delta b$  width. mbol  $\mathcal{N}$  in Eq. (13) denotes the volume concentration of the supercritical integration is carried out at any point of the blade surface upstream of the zone in the direction normal to this surface. Volume concentration  $\mathcal{N}$ wery rapidly with growing distance from the solid wall and Eq. (13) can maked by an approximate relationship

$$\Delta N = \kappa \mathcal{N}_0 w_1 \Delta b D \Delta t \tag{14}$$

is the concentration of the supercritical nuclei at the streamline coinciding blade section contour and D is a characteristic dimension of the machine diameter). The proportionality coefficient  $\kappa$  is assumed to depend excluthe velocity field pattern.

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Taking into account relationships (9), (10), (12) and (14) we can write down the volume loss per time unit as

$$\Delta V/\Delta t \propto (2\pi/3) \left(\Delta b/D\right) \left(K_1 - \lambda\right) \kappa \eta \mathcal{N}_0 \rho w_1^{-3} D^2 R_a^{-3} / \mathcal{R}_{cav} \propto \mathcal{N}_0 w_1^{-3} D^2 R_a^{-3} / \mathcal{R}_{cav}$$
(15)

In fact, erosion intensity depends often on a much higher power of relative velocity than that appearing in formula (15). A reasonable result can be obtained by making use of the analogy between the liquid impact and cavitation erosion mechanisms.

According to F. J. Heymann [21] the mean volume loss during a liquid impactest can be expressed as

$$\Delta V_{ii} = k'_{ii} \Delta N v^{4.26} \tag{15}$$

where  $\Delta N$  is the number of impacts, v — liquid jet velocity and  $k'_{ii}$  — a coefficient depending on material and jet parameters. Eq. (16) can be rewritten as

$$\Delta V/\Delta t = k_{li}'' v^{1.26} E_{kin} \mathcal{R}_{li}$$

where  $k_{li}^{\prime\prime}$  is a coefficient assumed constant for a definite facility and liquid use  $E_{kin} = 0.5\pi r^2 \rho v^3$  is the kinetic energy of a single liquid impact of duration  $\tau = \Delta t/\Delta r$  r — radius of the liquid jet and  $\Re_{li}$  — material resistance against liquid impact of duration  $\tau = \Delta t/\Delta r$  is a formula analogous to Eq. (10). Liquid compressibility and cosity as well as the liquid impact device size seem to be the basic parameters after the  $k_{li}^{\prime\prime}$  coefficient. A simple consideration based on the dimensional analymethods yields

$$\Delta V/\Delta t = k_{li} (cD/v) (v/c)^{1.26} E_{kin}/\mathcal{R}_{li}$$

where c and v denote the sound celerity and viscosity of the liquid, respective D is the characteristic size of the facility and  $k_{li}$  — a dimensionless parameter pending on the facility design, liquid impact kinematics and the "Reynolds number  $Re_c = cD/v$ . Although the precise form of the  $k_{li}$  coefficient dependence on the parameter is closely linked to the test device design, the physical intuition (erospirate fall with increasing liquid compressibility and viscosity) suggests that  $k_{li}$  show rise with growing  $Re_c$  at least as steeply as  $Re_c^{0.26}$ .

It can be easily seen from Eq. (18) that the efficiency of energy transfer in material appears proportional to  $v^{1.26}$ . Making use of previous assumptions at the analogy between the jet impact in a liquid impact test device and the cavitage microjet impact onto a solid wall, we can assume the coefficient  $\eta$  in Eq. (12) be proportional to  $\dot{R}_i^{1.26}$ . Taking Eq. (18) into account we obtain

$$\eta = k_{cav} \left[ 0.5(K_1 - \lambda) \sqrt{\frac{2\rho R_a^3 c^2}{34p_0 R_0^3}} \right]^{1.26} \left( \frac{w_1}{c} \right)^{2.52}$$

where  $k_{cav}$  is a dimensionless coefficient depending on the 2cr/v parameter with noting the microjet radius. Disregarding, in the first approximation, the r deme dence on the cavity and ambient liquid parameters we obtain  $k_{cav} = \text{const.}$  Here relationship (15) takes the form A Simplified Approach to Predict Some Cavitation Effects...

$$\left(\frac{\Delta V}{\Delta t}\right)_{cav} \propto k_{cav} \mathcal{N}_0 (K_1 - \lambda)^{2.26} \left(\frac{2\rho c^2 R_a^3}{3\Delta p_0 R_0^3}\right)^{0.63} \cdot \left(\frac{w_1}{c}\right)^{2.52} \rho w_1^{-3} D^2 R_a^{-3} / \mathcal{R}_{cav} = k_{cav} \mathcal{N}_0 (K_1 - \lambda)^{2.26} R_a^{-1.89} w_1^{-5.52} D^2 / \mathcal{R}_{cav}$$
(20)

mere

$$k'_{cav} = 0.775 \, k_{cav} \, \rho^{1.63} / (c^2 \varDelta p_0 R_0^3)^{0.63}.$$

Relationship (20) is valid only for kinematically similar flows which means

$$w_1 \propto c_1 \propto Q/D^2 \propto \sqrt{gH},$$
  
$$K_1 - \lambda \propto \Delta \sigma = \sigma_i - \sigma$$

and therefore

$$(\Delta V/\Delta t)_{cav} \propto k_{cav}'' \Delta \sigma^{2.26} \mathcal{N}_0 R_a^{4.89} D^2 H^{2.76} / \mathcal{R}_{cav}$$
(21)

iere

$$k''_{cav} = g^{2.76} k'_{cav}.$$

The scaling laws (20) and (21) require certain comments.

Proportionality between  $R_a$  and the runner diameter leads — in general — to exprediction of the size effect. In fact, such a proportionality may be assumed in case of very small  $\mathcal{N}_0$  and negligible interaction between cavitation bubbles. The erosion tests are carried out under such conditions. Furthermore, simple stereotical consideration indicates [12] that the maximum bubble radius should not be beeted to overstep the value

$$R_{\rm max} = 0.72 / \sqrt[3]{N_0}$$
.

This result has been confirmed by the experimental data of S. Mackiewicz [4] in the volume concentration of vapour in a cavitation cloud over a NACA 2418 to be always smaller than 65%.

The above consideration suggests that the size effect depends in general on supercal cavitation nuclei content. Erosion rate seems to be a very steeply growing from of size D and concentration  $\mathcal{N}_0$  for small nuclei contents and to grow proportionally to  $D^2$  and decrease slightly with growing  $\mathcal{N}_0$  for high nuclei ents. Numerous experimental data suggest the power exponent of the runner meter D to range between 3 and 5 [22] which is a sort of compromise between tendencies. On the other hand side, the scaling laws of N. I. Pylaev, Y. U. Edel' and A. S. Lashkov [24] as well as recent results of K. Steller [19] indicate the between 2 and 3 as most realistic.

The erosion rate dependence on the 5.5 power of velocity  $w_1$  in relationship (20) to be a reasonable result in view of the data of R. T. Knapp [18] and other the stress of the stressed that severe deviations in the value of the try power exponent are reported [19]. At least some of these deviations can be plained by the effect of the supercritical nuclei content  $\mathcal{N}_0$ . In fact  $\mathcal{N}_0$  depends the critical nuclei radius

$$R_{cr} = 2s/(p_v - p_{\min}) \tag{22}$$

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where  $p_v - p_{\min} = 0.5\rho w_1^2 (K_1 - \lambda) = \Delta \sigma \rho g H$ ,  $p_{\min}$  is the minimum pressure at the blade section contour and s denotes the surface tension coefficient. It is quite evident that the function  $\mathcal{N}_0 = \mathcal{N}_0(R_{cr})$  can be replaced by a function of relative velocity wor total head H. The course of these functions is defined by the cavitation nucle spectra which usually differ between different test facilities.

#### 4. Conclusions

Despite of far reaching simplifications, the model of single bubble evolution a described in Ref. [13] proved a reliable tool for prediction of cavitation erosize zones under field conditions.

Single bubble model and some data from the liquid impact erosion tests we used in Ref. [14] and the present report to derive a scaling law on cavitation erosion. The result is close to that of other authors although size effect seems to depend essentially on the cavitation nuclei spectra. Experimental verification of this set tement is needed.

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### Uproszczone metody przewidywania niektórych efektów kawitacyjnych na łopatkach wirników osiowych

#### Streszczenie

Praca stanowi przegląd dwóch uproszczonych metod rozwiniętych ostatnio przez obu autorów, oceny różnych aspektów kawitacji w wirnikach maszyn hydraulicznych. Podano podstawowe nenia uproszczonego modelu ewolucji pojedynczego pęcherzyka, opisanego szczegółowo w podnich pracach. Stosowalność tego modelu do przewidywania strat erozji na profilach łopatkowych trowano na przykładzie turbiny Kaplana w Elektrowni Wodnej Bergheim na niemieckim odcinku naju. Następnie, posługując się podobnymi założeniami a także pewnymi wynikami badań erozji zającą strugą, wyprowadzono prawo skalowania erozji kawitacyjnej. Wynik jest podobny do kanego poprzednio innymi metodami przez innych autorów, chociaż wpływ rozmiaru maszyny się mocno zależeć od widma jąder kawitacyjnych. Konieczna jest doświadczalna weryfikacja stwierdzenia.

### Упрощённые методы предвидывания некоторых кавитационных эффектов на лопатках осевых роторов

#### Резюме

Реферат является просмотром двух упрощённых методов, развитых за последнее время обома рами, в целью оценки аспектов кавитации в роторах гидравлических машин. Представлены вные предположения упрощённой модели эволюции одиночного пузырька, подробно описанной рами, трудах. Применяемость этой модели для предвидывания эрозионных зон на лопаых профилях иллюстрируется на примере турбины Каплана в Гидроэлектростанции Берггейм срманском участке Дуная. Затем, пользуясь похожими предположениями, а также некоторыми пьтатами исследований эрозии ударяющей струей, выводится закон калибровки кавитационэрозии. Результат похож на достигнутый раньше другими методами другими авторами, хотя ние размера машины кажется быть сильно зависящим от сектора кавитационных ядер. бходима экспериментальная верификация этого обнаружения.