Comparison of mathematical models concerning methane fermentation process of selected potato biomass wastes

Krzysztof PIOTROWSKI Department of Chemical Engineering and Process Design Silesian University of Technology in Gliwice

Jan CEBULA The University of Bielsko-Biała Institute of Environmental Protection and Engineering

Jolanta BOHDZIEWICZ, Anna DUDEK

Institute of Water and Wastewater Engineering Silesian University of Technology in Gliwice

### INTRODUCTION



Catering industry wastes - one of possible main, abundant sources of substrates for biogas plants

Dominant fraction of these wastes will be represented by potatoes

Subject of various methods of thermal processing, strongly influencing their structure, composition, thus smaller or higher ability for their decomposition in anaerobic fermentation process

Photos: https://www.google.pl/search







#### **AIM AND SCOPE**

1. Potential and kinetic aspects of batch methane fermentation process of:

- fried chips
- boiled potatoes
  - fried potatoes

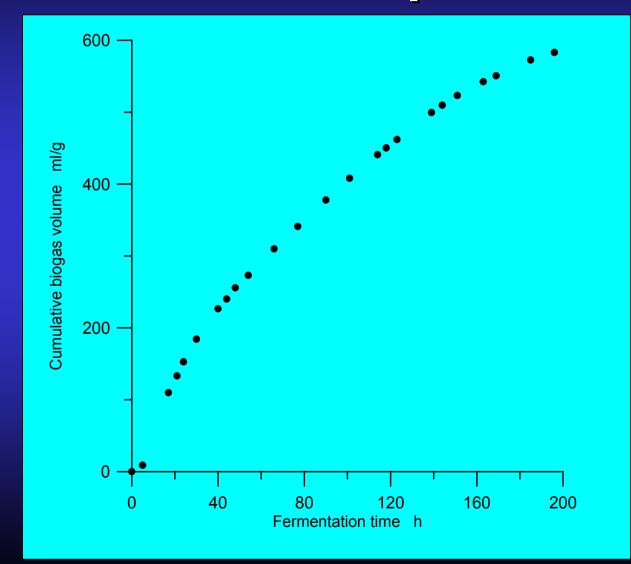
2. Comparison of applicability of selected literature kinetic models

## Experimental

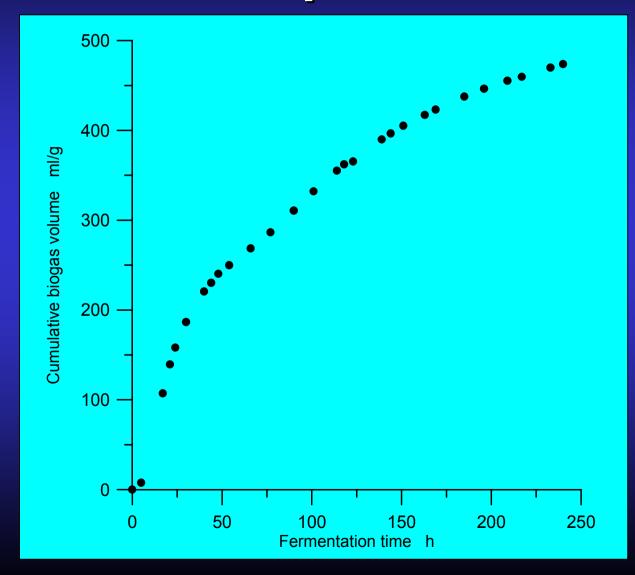




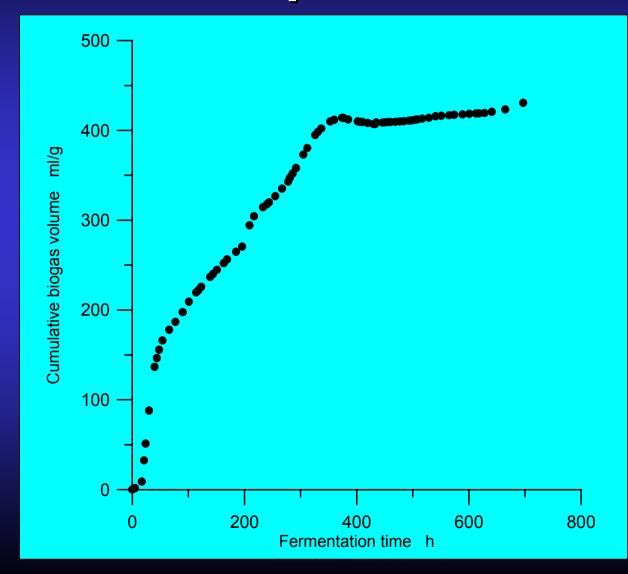
## **Fried chips**



## **Boiled potatoes**



## **Fried potatoes**



# **Kinetic models**

#### Modified Gompertz model

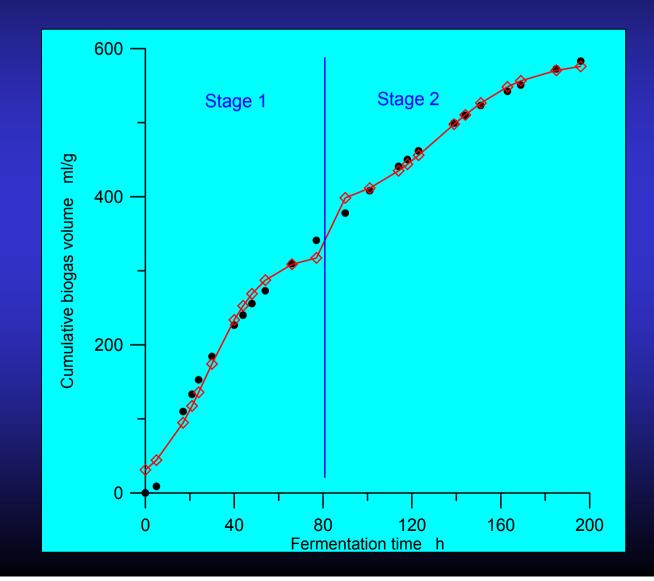
#### and other ones...

Modified Logistic model Exponential model Fitzhugh model Cone model

$$H = H_{\max} \exp\left\{-\exp\left[\frac{R_{\max}e}{H_{\max}}(\lambda - t) + 1\right]\right\}$$
$$H = \frac{H_{\max}}{1 + \exp\left[\frac{4R_{\max}(\lambda - t)}{H_{\max}} + 2\right]}$$
$$H = H_{\max}\left(1 - \exp\left(-kt\right)\right)$$
$$H = H_{\max}\left(1 - \exp\left(-kt\right)^{n}\right)$$
$$H = \frac{H_{\max}}{\left(1 + \left(kt\right)^{-n}\right)}$$

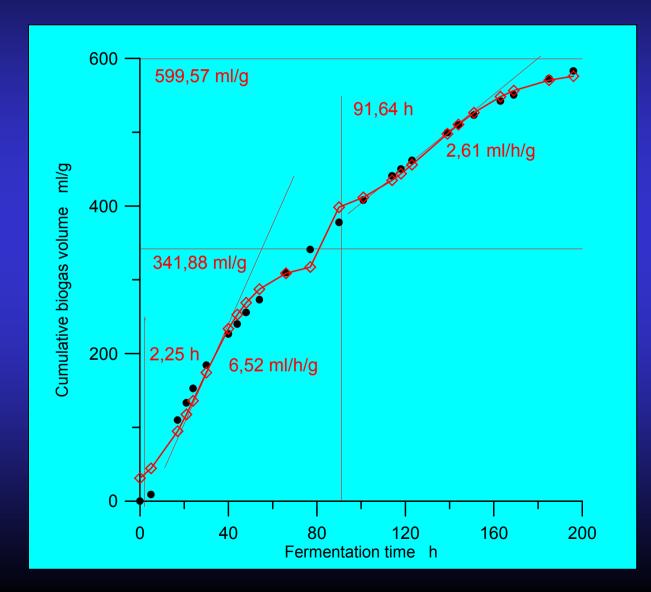
## **Fried chips**

Modified Gompertz model



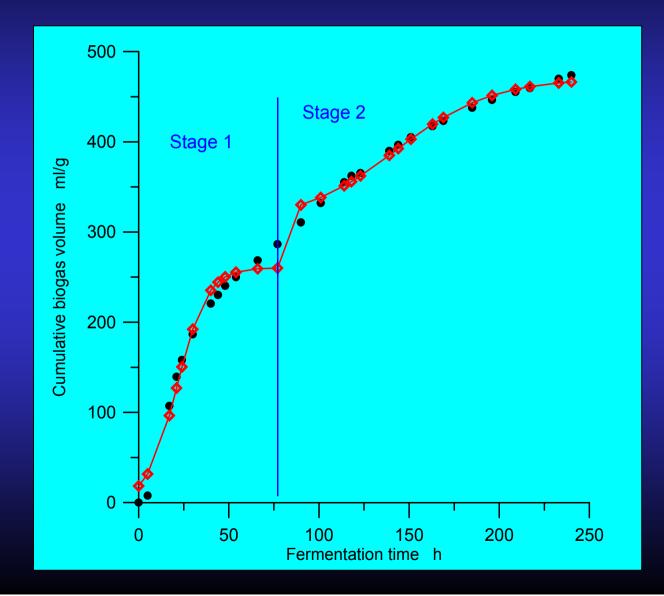
## **Fried chips**

Modified Gompertz model



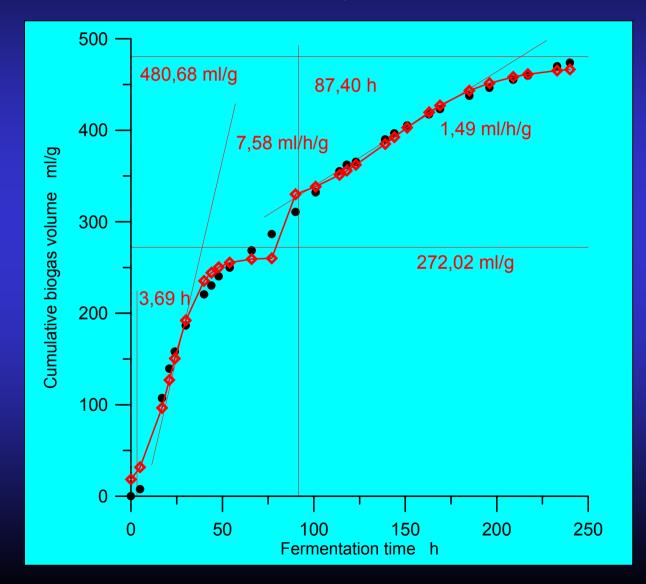
## **Boiled potatoes**

Modified Gompertz model



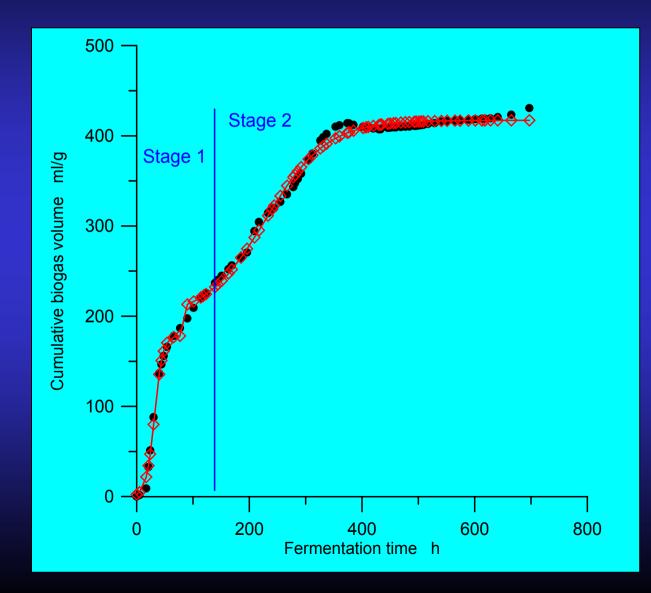
## **Boiled potatoes**

Modified Gompertz model



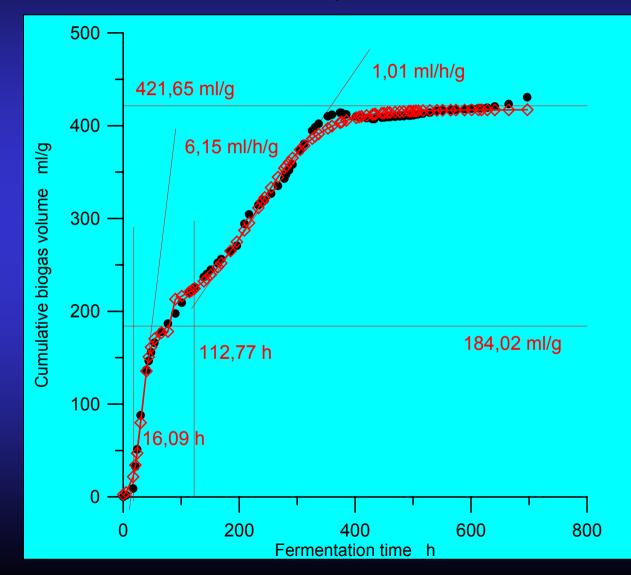
## **Fried potatoes**

Modified Gompertz model



## **Fried potatoes**

Modified Gompertz model



### **Kinetic models - discussion**

The most suitable equation modeling characteristic, sigmoid-shape course of H(t) is modified Gompertz model.

Logistic model demonstrates lower abilities of experimental data fitting what directly affects the accuracy of  $H_{max}$ ,  $R_{max}$  and  $\lambda$  values.

Exponential model, Fitzhugh model and Cone model provide one with significantly too high  $H_{max}$  values, what results from mathematical difficulties in proper rendering the characteristic timecourse H(t) of experimental data (sigmoid).

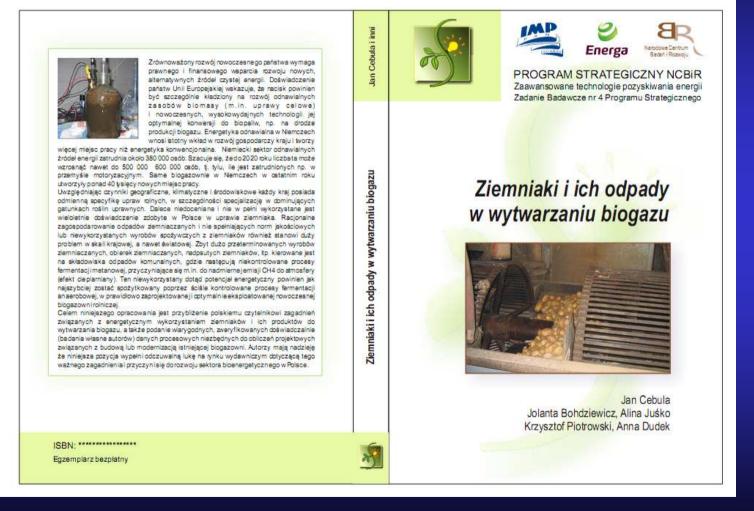
From the modified Gompertz model and Logistic model one can obtain set of parameters  $H_{max}$ ,  $R_{max}$ ,  $\lambda$  of direct practical applicability.

The parameter values resulting from both models are quite similar.

#### Conclusions

- 1. Batch methane fermentation process of the three potato biomass wastes discussed is the best mathematically described by modified Gompertz kinetic model.
- 2. The highest potential in biogas production is attributed to fried chips wastes (the highest  $H_{\text{max}}$  and relatively high  $R_{\text{max}}$  both in 1 and in 2 stage, the shortest total time of the integrated 2-stage process (ca. 200 h)).
- 3. Relatively the least suitable substrate are fried potatoes wastes (the lowest  $H_{max}$  after ca. 700 h), simultaneously at the smallest methane fermentation rate  $R_{max}$ .

#### More details soon in...



## Thank You for attention